

# IMPORTANT—FORMULAS

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**1.**  $\int 1 \, dx = x$

**2.**  $\int c \, dx = cx$

**3.**  $\int x^n \, dx = \frac{x^{n+1}}{n+1}$

**4.**  $\int \frac{1}{x} \, dx = \ln|x|$

**5.**  $\int [f(x)]^n f'(x) \, dx = \frac{[f(x)]^{n+1}}{n+1}$

**6.**  $\int [f(x)]^{-1} f'(x) \, dx = \ln f(x)$

**7.**  $\int e^x \, dx = e^x$

**8.**  $\int a^x \, dx = \frac{a^x}{\ln a}$

**9.**  $\int \sin x \, dx = -\cos x$

**10.**  $\int \sin kx \, dx = -\frac{\cos kx}{k}$

**11.**  $\int \cos x \, dx = \sin x$

**12.**  $\int \cos kx \, dx = \frac{\sin kx}{k}$

**13.**  $\int \sec^2 x \, dx = \tan x$

**14.**  $\int \operatorname{cosec}^2 x \, dx = -\cot x$

**15.**  $\int \sec x \tan x \, dx = \sec x$

**16.**  ~~$\int \operatorname{cosec} x \cot x \, dx = -\operatorname{cosec} x$~~

**17.**  $\int \tan x \, dx = \ln|\sec x|$

**18.**  $\int \cot x \, dx = \ln|\sin x|$

**19.**  $\int \sec x \, dx = \ln|\sec x + \tan x|$

**20.**  ~~$\int \operatorname{cosec} x \, dx = \ln|\operatorname{cosec} x - \cot x|$~~

**21.**  $\int \frac{1}{x^2-a^2} \, dx = \frac{1}{2a} \ln \left| \frac{x-a}{x+a} \right|$

**22.**  $\int \frac{1}{a^2-x^2} \, dx = \frac{1}{2a} \ln \left| \frac{a+x}{a-x} \right|$

**23.**  $\int \frac{1}{\sqrt{x^2+a^2}} \, dx = \ln|x + \sqrt{x^2+a^2}|$

**24.**  $\int \frac{1}{\sqrt{x^2-a^2}} \, dx = \ln|x + \sqrt{x^2-a^2}|$

**25.**  $\int \frac{1}{\sqrt{a^2-x^2}} \, dx = \sin^{-1}\left(\frac{x}{a}\right) \quad OR \quad -\cos^{-1}\left(\frac{x}{a}\right)$

**26.**  $\int \frac{1}{a^2+x^2} \, dx = \frac{1}{a} \tan^{-1}\left(\frac{x}{a}\right) \quad OR \quad -\frac{1}{a} \cot^{-1}\left(\frac{x}{a}\right)$

**27.**  $\int \frac{1}{x\sqrt{x^2-a^2}} \, dx = \sec^{-1}\left(\frac{x}{a}\right) \quad OR \quad -\csc^{-1}\left(\frac{x}{a}\right)$

**28.**  $\int \sqrt{a^2-x^2} \, dx = \frac{x\sqrt{a^2-x^2}}{2} + \frac{a^2}{2} \sin^{-1}\left(\frac{x}{a}\right)$

**29.**  $\int \sqrt{x^2+a^2} \, dx = \frac{x\sqrt{x^2+a^2}}{2} + \frac{a^2}{2} \ln \left| \frac{x\sqrt{x^2+a^2}}{a} \right|$

**30.**  $\int \sqrt{x^2-a^2} \, dx = \frac{x\sqrt{x^2-a^2}}{2} - \frac{a^2}{2} \ln \left| \frac{x\sqrt{x^2-a^2}}{a} \right|$