
Govt. Ghazali Degree College, Jhang

(Important Short Questions)

Course: Calculus and Analytic Geometry

Chapter # 03

Integration

Following short questions are selected from previous 5 years papers of different boards. Solve these at your own to perform well in annual exams.

1. Using differential, find $\frac{dy}{dx}$, if $xy - \ln x = c$.
2. Using differential, find $\frac{dy}{dx}$, when $\frac{y}{x} - \ln x = \ln c$.
3. Use differential to approximate the value of $\sqrt[4]{17}$.
4. Use differential to approximate the value of $(31)^{\frac{1}{5}}$.
5. Use differential to find $\frac{dy}{dx}$ for $x^2 + 2y^2 = 16$.
6. Find δy if $y = x^2 + 2x$ when x changes from 2 to 2.18.
7. Find δy and dy if $y = \sqrt{x}$, when x changes from 4 to 4.41.
8. If $y = x^2 - 1$, find δy and dy when x changes from 3 to 3.02.
9. Evaluate $\int (\sqrt{x} - \frac{1}{x}) dx$, $x > 0$.
10. Evaluate $\int \sin(a + b)x dx$.
11. Evaluate $\int \ln x dx$.
12. Evaluate $\int \frac{e^{2x} + e^{2x}}{e^x} dx$.
13. Evaluate $\int_{-2}^0 \frac{1}{(2x-1)^2} dx$.
14. Evaluate $\int_0^2 (e^{\frac{x}{2}} - e^{-\frac{x}{2}}) dx$.
15. Evaluate $\int \cos 3x \sin 2x dx$.
16. Evaluate $\int \sqrt{\frac{1+x}{1-x}} dx$.
17. Evaluate $\int \frac{x+2}{\sqrt{x+3}} dx$.
18. Evaluate $\int x^3 \tan^{-1} x dx$.
19. Evaluate $\int \sec^4 x dx$.
20. Evaluate $\int_{-1}^5 |x - 3| dx$.
21. Evaluate $\int \frac{(a-b)x}{(x-a)(x-b)} dx$.

22. Evaluate $\int_0^1 \frac{3x}{4-3x} dx$.
23. Evaluate $\int (x-1)(x-3) dx$.
24. Evaluate $\int (\ln x)^{\frac{1}{x}} dx$, $x > 0$.
25. Evaluate $\int \sec x dx$.
26. Evaluate $\int (\ln x)^2 dx$.
27. Evaluate $\int_1^2 \frac{x}{x^2+2} dx$.
28. Evaluate $\int \frac{x+2}{\sqrt{x+3}} dx$.
29. Evaluate $\int \frac{2a}{x^2-a^2}, x > 0$.
30. Evaluate $\int \sqrt{1+\sin x} dx$.
31. Evaluate $\int x e^x dx$.
32. Evaluate $\int_1^2 \ln x dx$.
33. Evaluate $\int \frac{dx}{\sqrt{x+1}-\sqrt{x}}$.
34. Evaluate $\int \sqrt{1-\cos 2x} dx$, $(1-\cos 2x < 0)$.
35. Evaluate $\int \frac{dx}{a^2-x^2} dx$, $(x > 0)$.
36. Evaluate $\int [x + |x|] dx$.
37. Evaluate $\int_0^3 \frac{dx}{x^2+9}$.
38. Evaluate $\int (a-2x)^{\frac{3}{2}} dx$.
39. Evaluate $\int x \sqrt{x^2-1} dx$.
40. Evaluate $\int \frac{(\sqrt{x-1})^2}{\sqrt{x}} dx$.
41. Evaluate $\int \tan^2 x dx$.
42. Evaluate $\int \frac{adt}{2\sqrt{at+b}}$.
43. Evaluate $\int x \ln x dx$.
44. Evaluate $\int_0^{\frac{\pi}{4}} \sec x (\sec x + \tan x) dx$.
45. Evaluate $\int_{-6}^2 \sqrt{3-x} dx$.
46. Evaluate $\int_0^{\frac{\pi}{4}} \frac{1}{1-\sin x} dx$.
47. Evaluate $\int \frac{2x}{x^2-a^2} dx$.
48. Evaluate $\int \frac{1-x^2}{1+x^2} dx$.

49. Evaluate $\int \frac{\sec^2 x}{\sqrt{\tan x}} dx$.
50. Evaluate $\int \frac{x}{\sqrt{x+x^2}} dx$.
51. Evaluate $\int x^2 \ln x dx$.
52. Evaluate $\int x \cos x dx$.
53. Evaluate $\int \frac{1}{x \ln x} dx$.
54. Evaluate $\int \tan^{-1} x dx$.
55. Evaluate $\int (x^{3+3x^2}) dx$.
56. Evaluate $\int_0^4 \frac{\sin x - 1}{\cos^2 x} dx$.
57. Evaluate $\frac{3 - \cos 2x}{1 + \cos 2x} dx$.
58. Evaluate $\int \frac{\cot \sqrt{x}}{\sqrt{x}} dx$.
59. Evaluate $\int x^2 a e^{ax} dx$.
60. Evaluate $\int (\ln x)^2 dx$.
61. Evaluate $\int \frac{e^x (x^2 + 1)}{(x+1)^2} dx$.
62. Evaluate $\int \frac{ax+b}{ax^2+2bx+c} dx$.
63. Evaluate $\int \frac{e^x}{e^x+3} dx$.
64. Evaluate $\int x \sin x dx$.
65. Evaluate $\int e^x (\cos x + \sin x) dx$.
66. Evaluate $\int \frac{7x-1}{(x-1)(x+1)} dx$.
67. Evaluate $\int_1^{\sqrt{5}} \sqrt{(2t-t)^3} dt$.
68. Prove that $\int_a^b f(x) dx = \int_a^c f(x) dx + \int_c^b f(x) dx$ where $a < c < b$.
69. If $\int_{-2}^1 f(x) dx = 5$, $\int_{-2}^1 g(x) dx = 4$, then evaluate $\int_{-2}^1 (2f(x) + 3g(x)) dx$.
70. Find the area bounded by $y = \cos x$ from $x = -\frac{\pi}{2}$ to $x = \frac{\pi}{2}$.
71. Find the area between x -axis and the curve from $x = 1$ to $x = 2$.
72. Find the area between the x -axis and the curve, $y = 4x - x^3$.
73. Find the area between x -axis and the curve $y = \sin 2x$ from $x = 0$ to $x = \frac{\pi}{3}$.
74. Find the area bounded by the curve $y = 4 - x^2$ and x -axis.
75. Find the area bounded by $y = \cos$ from $x = -\frac{\pi}{2}$ to $x = \frac{\pi}{2}$.

76. Find the area between x - *axis* and the curve $y = 4x - x^2$.
77. Solve the differential equation $(x - 1)dx + ydy = 0$.
78. Solve the differential equation $x^2(2y + 1)\frac{dy}{dx} - 1 = 0$.
79. Solve the differential equation $\frac{dy}{dx} = \frac{1-x}{y}$.
80. Solve the differential equation $(\sin y + y \cos y)dy = [x(2 \ln x + 1)]dx$
81. Solve the differential equation $\frac{dy}{dx} + \frac{2xy}{2y+1} = x$.
82. Solve the differential equation $\frac{dy}{dx} = \frac{y^2+1}{e^{-x}}$.

Best of Luck

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by

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